# Pre-Calculus - Chapter 2 Study Guide

This is a summary of Chapter 2. The indicated Section problems are meant as a quideline to the type of problems that are on the test. You <u>DO NOT</u> have to do all of them. It is suggested to do a couple or more (as needed) from the odds and check the answers on the back of the book. If you feel confident on a given section, skip it and concentrate on those sections where you feel you need the most help.

### 2.1- Operations with Complex Numbers a + bi

- Vertex.  $x = \frac{b}{2a}$  then plug in "x" to find "y". The vertex is a point.
  - Find the intercepts: x-int  $\rightarrow$  set y = 0 y-int $\rightarrow$  set x = 0.
  - Find the equation and graph the axis of symmetry.  $x = \frac{-b}{2a}$  The axis of symmetry is a line. •
  - Graph the vertex, and intercepts. Use reflection to graph additional points. There should be at least 5 ٠ points, unless otherwise indicated. (There may be more points requested on the test). Graph the parabola. (Must look symmetric about the axis of symmetry).
  - The Maximum is the y-value of the highest point. ٠
  - The Minimum is the y-value of the lowest point. •
  - The Domain is all the possible x-values. For parabolas opening up or down, the Domain is  $(-\infty,\infty)$ .
  - The Range is all the possible y-values from [Max/Min]. It varies depending on the parabola. •

#### 2.2- Maximum Area Prob. $\rightarrow$ (#65-70)

- Include drawing.
- Use the equation for the length of the fence and the equation of the Area, either A(I) or A(w).
- Find the vertex. → X-Value will be length or width. Y-Value will be the MAX AREA
- Find the other dimension with the correct units.

#### 2.3- Graphing Polynomial Functions: Prob. $\rightarrow$ (#41-63)

- Find all the zeros by factoring and setting = 0 •
  - Use the Fundamental Theorem of Algebra to determine if you have the correct number of solutions. The degree of the polynomial = number of solutions. Remember that solutions could be repeated. Ex. x = 3, x = 3, x = 1 count as 3 solutions. Therefore the polynomial's degree = 3.
- Find the y-intercept. Set x = 0. •
- Approximate the Critical Points.
- Use the end-behavior and the number of turns (n-1) to graph.

#### 2.4- Finding the zeros of Polynomial Functions, Remainder and Factor Theorems: Prob. $\rightarrow$ (#1-45)

- Practice dividing polynomials using Long and Synthetic Division. •
- The Remainder Theorem (If a polynomial is divided by (x c), then f(c) = Remainder) ٠
- The Factor Theorem (If f(c) = 0, then (x c) is a factor of the polynomial.) ٠

#### 2.5-Using the Rational Root Theorem to find the rational zeros of Polynomial Functions. Finding All the Zeros of Polynomial Functions. Prob. $\rightarrow$ (#1-37).

- Find the possible rational zeros  $\left(\frac{P}{\rho}'s\right)$  Rational Root Theorem •
- Find one that works using the remainder and factor theorems. Ex: If f(2) = 0, then x 2 is a factor.
- Use synthetic division to find the remaining factors to factor completely.
- Set each factor = 0 and solve. ٠

- If a <u>quadratic factor</u> does not factor further, then use the quadratic formula to solve it. This will give you 2 zeros that are either irrational or imaginary. Only the  $(\frac{P}{O}'s)$  will give you the *possible rational zeros*.
- Find the zeros.

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• Use *Descartes's Rule of Signs* to determine the possible real positive and the possible real negative zeros.

# 2.6- Graphing Rational Functions: Prob. $\rightarrow$ (#57-87). (Also review the study guide for 2.6)

- <u>Find the Vertical Asymptote</u>(s): **(VA)** and **Holes**. [These exist if and only if there is a <u>Domain Restriction</u>] \*\*\*Factor the numerator and denominator:
  - If any factor from the denominator cancels with factors from the numerator, set = 0 and that will give you the x-value [Domain Restr.] of a *hole* in the graph. To find the y-value, plug in the x-value into f(x). The holes are points (x,y). \*\*remember to simplify F(x) before finding the y-value
  - Factors from the denominator that do not cancel will become <u>Vertical Asymptotes</u>. Set = 0 and solve for x→ Domain restriction(s) that are not Holes.
  - There may be no Vertical Asymptote or several Vertical Asymptotes. Technically, there is no limit to the number of Vertical Asymptotes in Polynomial Functions.
  - Note: Vertical Asymptotes are lines, therefore the equation will be x = Domain Restr.
- <u>Finding Horizontal Asymptote</u>: **(HA)** if any. (y = constant). Rules:
  - 1- If the degree of the numerator < the degree of the denominator, then y = 0. [x-axis]
  - 2- If the degree of the numerator = the degree of the denominator, then  $y = \frac{LC Num}{LC D m}$
  - $\circ$  3- If the degree of the numerator > the degree of the denominator, **then** <u>NO HA</u>.
  - There can be 0 or 1 Horizontal Asymptote.
  - $\circ$  Note: The Horizontal Asymptote is a line, therefore the equation will be y = #
- Finding Slant Asymptote: (SA)
  - If the degree of the numerator > the degree of the denominator <u>by exactly one unit</u>, then there is a Slant Asymptote.
  - $\circ$   $\;$  Use synthetic or long division to divide.
  - The Slant Asymptote will be **y** = **quotient of the division**. *Disregard the remainder*.
  - Note: The Slant Asymptotes is a line, therefore the equation is y = quotient of the division
- Find the y-intercept: set x = 0 and solve.
- Find the x-intercept(s): set f(x) = 0 and solve. [set -numerator--p(x) = 0]
- Use tables of values with at least 3 points each to the *left, right*, and *between Vertical Asymptotes*. Try to use x values close to the asymptotes.
  - $\circ$  Graph the branches.

# 2.7-Solve polynomial and rational inequalities: Prob. $\rightarrow$ (#1-59)

- Find the zeros and Domain restriction(s) (if any).
- Draw a number line with intervals including the *zeros* and *restrictions*.
  - $\circ$   $\;$  Test values of "x" on each interval.
  - (Parenthesis) for  $\infty$ ,  $-\infty$ , restrictions and if function contains > or <.
  - [Brackets] for zeros if function contains ≤  $or \ge$ .
- Test values of "x" on each interval.
- Write the solution by selecting the interval(s) that satisfy the given function.

# 2.8- Prob. → #94, 95, 97 Modeling with variation

- Direct variation: y = kx
- Inverse variation:  $y = {}^{k}$
- Joint variation: y=k(a)(b)(c)
- Combined variation: combination of direct, inverse and/or joint.