## Transformations

## Translations

1) Using the translation $(x, y) \rightarrow(x-4, y+3)$, find the image of the given points.

$$
G(-2,4) \quad H(-10,5)
$$

2) Segment $F G$ with endpoints $F(0,-3)$ and $G(0,-1)$ is translated 2 units up and 3 units to the left, find the coordinates of $F^{\prime}$ and $G^{\prime}$ and write the rule for this transformation.
3) Segment $X Y$ with endpoints $X(2,-3)$ and $Y(-3,1)$ is translated 4 units down and 1 unit to the right, find the coordinates of $X^{\prime}$ and $Y^{\prime}$ and write the rule for this transformation.
4) The vertices of $\Delta J K L$ are $J(-2,8), K(1,-3)$, and $L(5,4)$. If $\Delta J K L$ is transformed following the rule $(x, y) \rightarrow(x+$ $6, y-1)$, what are the coordinates of the vertices of $\Delta J^{\prime} K^{\prime} L^{\prime}$ ?
5) Maggie transformed $\triangle A B C$ with vertices $A(-3,5), B(-2,2)$, and $C(-4,2)$ onto $\Delta A^{\prime} B^{\prime} C^{\prime}$ with vertices $A^{\prime}(3,1)$, $B^{\prime}(4,-2)$, and $C^{\prime}(2,-2)$. Write a rule that maps $\triangle A B C$ onto $\triangle A^{\prime} B^{\prime} C^{\prime}$.
6) What is the rule that maps $\Delta H I J$ onto $\Delta H^{\prime} I^{\prime} J^{\prime}$ ?

A. $(x, y) \rightarrow(x+2, y+4)$
B. $(x, y) \rightarrow(x-2, y-4)$
C. $(x, y) \rightarrow(x+4, y+2)$
D. $(x, y) \rightarrow(x-4, y-2)$

## Reflections

7) Segment $F G$ with endpoints $F(0,-3)$ and $G(0,-1)$ is reflected over the $x$-axis, find the coordinates of $F^{\prime}$ and $G^{\prime}$ and write the rule for this transformation.
8) Segment $X Y$ with endpoints $X(2,-3)$ and $Y(-3,1)$ is reflected over the $y$-axis, find the coordinates of $X^{\prime}$ and $Y^{\prime}$ and write the rule for this transformation.

## Transformations

9) Segment $P Q$ with endpoints $P(2,-3)$ and $Q(-3,1)$ is reflected over the line $y=x$, find the coordinates of $P^{\prime}$ and $Q^{\prime}$ and write the rule for this transformation.
10) Segment $T S$ with endpoints $T(-4,6)$ and $S(2,-1)$ is reflected over the line $y=-x$, find the coordinates of $T^{\prime}$ and $S^{\prime}$ and write the rule for this transformation.
11) What transformation maps the Preimage onto the Image?

A. Reflection over the line $y=0$
B. Reflection over the line $x=0$
C. Reflection over the line $y=x$
D. Reflection over the line $y=-x$

## Rotations

12) Segment $F G$ with endpoints $F(1,-3)$ and $G(2,-1)$ is rotated $90^{\circ}$ clockwise about the origin, find the coordinates of $F^{\prime}$ and $G^{\prime}$ and write the rule for this transformation.
13) Segment $X Y$ with endpoints $X(2,-3)$ and $Y(-3,1)$ is rotated $90^{\circ}$ counterclockwise about the origin, find the coordinates of $X^{\prime}$ and $Y^{\prime}$ and write the rule for this transformation.
14) Segment $P Q$ with endpoints $P(2,-3)$ and $Q(-3,1)$ is rotated $180^{\circ}$ about the origin, find the coordinates of $P^{\prime}$ and $Q^{\prime}$ and write the rule for this transformation.
15) Segment $T S$ with endpoints $T(-4,6)$ and $S(2,-1)$ is rotated $270^{\circ}$ clockwise about the origin, find the coordinates of $T^{\prime}$ and $S^{\prime}$ and write the rule for this transformation.
16) Segment $M N$ with endpoints $M(7,-2)$ and $N(-5,4)$ is rotated $270^{\circ}$ counterclockwise about the origin, find the coordinates of $M^{\prime}$ and $N^{\prime}$ and write the rule for this transformation.

## Transformations

17) Given triangle $A B C$ with vertices $A(-1,0), B(-3,-4)$, and $C(-4,-1)$, write the coordinates of its image, triangle $A^{\prime} B^{\prime} C^{\prime}$, after a rotation of $270^{\circ}$ clockwise about the origin.
A. $A^{\prime}(1,0), B^{\prime}(3,4)$, and $C^{\prime}(4,1)$
B. $A^{\prime}(-1,0), B^{\prime}(-3,4)$, and $C^{\prime}(-4,1)$
C. $A^{\prime}(0,1), B^{\prime}(4,3)$, and $C^{\prime}(1,4)$
D. $A^{\prime}(0,-1), B^{\prime}(4,-3)$, and $C^{\prime}(1,-4)$
18) Quadrilateral $A B C D$ is rotated $90^{\circ}$ about the origin. What will be the coordinates of $D^{\prime}$ ?

A. $D^{\prime}(-1,-4)$
B. $D^{\prime}(-4,-1)$
C. $D^{\prime}(1,4)$
D. $D^{\prime}(4,1)$

## Dilations

19) What are the coordinates of the image of segment $M N$ with endpoints $M(4,-2)$ and $N(-3,5)$ after a dilation with scale factor 3 and the origin as the center of dilation? Write the rule for this transformation.
20) What are the coordinates of the image of segment $J K$ with endpoints $J(4,0)$ and $K(-12,3)$ after a dilation with scale factor $\frac{1}{4}$ and the origin as the center of dilation? Write the rule for this transformation.
21) What are the coordinates of the image of segment $C V$ with endpoints $C(3,2)$ and $V(1,-6)$ after a dilation with scale factor $\frac{3}{2}$ and the origin as the center of dilation? Write the rule for this transformation.
22) Triangle $A B C$ with vertices $A(-2,1), B(-2,-1)$, and $C(2,-2)$ is transformed following the rule $(x, y) \rightarrow(2 x, 2 y)$. What are the coordinates of its image, triangle $A^{\prime} B^{\prime} C^{\prime}$ ?
A. $A^{\prime}(-2,2), B^{\prime}(-2,-2)$, and $C^{\prime}(2,-4)$
B. $A^{\prime}(2,-2), B^{\prime}(2,2)$, and $C^{\prime}(-2,4)$
C. $A^{\prime}(-4,1), B^{\prime}(-4,-1)$, and $C^{\prime}(4,-2)$
D. $A^{\prime}(-4,2), B^{\prime}(-4,-2)$, and $C^{\prime}(4,-4)$

## Transformations

23) Consider $\triangle A B C$ and its image. Which statement describe the dilation?

A. Dilation centered at the origin with a scale factor of 2 .
B. Dilation centered at the origin with a scale factor of $\frac{1}{2}$.
C. Dilation centered at $C$ with a scale factor of 2 .
D. Dilation centered at $C$ with a scale factor of $\frac{1}{2}$.

## Practice

24) Consider quadrilateral $A B C D$ and its image. Which statement describes the transformation?

A. Rotation of $180^{\circ}$ counterclockwise about the origin.
B. Reflection over the line $x=2$.
C. Translation of 4 units down.
D. Reflection over the line $y=2$.
25) Consider quadrilateral $A B C D$ and its image. Which statement describe the transformation?

A. Reflection in the $y$-axis
B. Rotation $180^{\circ}$ about point $C$.
C. Reflection in the line $x=-2$.
D. Translation of 4 units to the right.
26) Triangle $C D E$ has vertices $C(-3,5), D(-2,2)$, and $E(-4,2)$. If $\triangle C D E$ is transformed by a dilation centered in $D$ with a scale factor of $\frac{1}{4}$ followed by a rotation of $90^{\circ}$ clockwise about the origin, what will be the coordinates of the final image of point $C$ after the two transformations?
A. $(-6,3)$
B. $(-4,4)$
C. $(-2.25,2.75)$
D. $(2.75,2.25)$

## Transformations

27) On the set of axes below, $\triangle D O G \cong \triangle C A T$. Which sequence of transformations maps $\triangle D O G$ onto $\triangle C A T$ ?

A. A translation of 5 units down followed by a reflection over the $y$-axis.
B. A translation of 5 units up followed by a reflection over the $y$ axis.
C. A translation of 6 units to the right followed by a reflection over the $x$-axis.
D. A translation of 6 units to the left followed by a reflection over the $x$-axis.
28) On the set of axes below, $\triangle L E T$ and $\Delta L " E " T$ " are graphed in the coordinate plane where $\Delta L E T \cong \Delta L " E " T "$. Which sequence of rigid motions maps $\triangle L E T$ onto $\Delta L " E " T "$ ?

A. a reflection over the $y$-axis followed by a reflection over the $x$ axis.
B. a rotation of $180^{\circ}$ about the origin.
C. a rotation of $90^{\circ}$ counterclockwise about the origin followed by a reflection over the $y$-axis.
D. a reflection over the $x$-axis followed by a rotation of $90^{\circ}$ clockwise about the origin.
29) Triangle $B A T$ has vertices $B(2,1), A(6,2)$, and $T(3,6)$. If $\triangle B A T$ is transformed by a rotation of $270^{\circ}$ counterclockwise about the origin followed by a translation with rule $(x, y) \rightarrow(x+3, y+6)$, what will be the coordinates of the final image of point $A$ after the two transformations?
A. $(2,-6)$
B. $(5,0)$
C. $(6,-3)$
D. $(9,3)$

## Transformations

30) Triangle TUV is shown on this coordinate plane.


Triangle $T U V$ will be reflected over the $x$-axis.
The image of triangle $T U V$ will then be translated 2 units up and 1 unit left.
What will be the coordinates of the final image of point $V$ after the two transformations?
A. $(0,4)$
B. $(4,0)$
C. $(4,-6)$
D. $(-6,4)$
31) Given $\triangle A B C$ and its image $\triangle A^{\prime} B^{\prime} C^{\prime}$. Which transformation(s) maps $\triangle A B C$ onto $\triangle A^{\prime} B^{\prime} C^{\prime}$ ? Select All that apply.

A. Rotation $90^{\circ}$ counterclockwise about the origin.
B. Rotation $90^{\circ}$ clockwise about the origin.
C. $(x, y) \rightarrow(-x,-y)$
D. Rotation $270^{\circ}$ clockwise about the origin.
E. $(x, y) \rightarrow(-y, x)$
F. Rotation $270^{\circ}$ counterclockwise about the origin.
G. $(x, y) \rightarrow(y,-x)$
32) The vertices of $\triangle A B C$ are $A(-1,2), B(3,3)$, and $C(2,5)$. What are the vertices of $\triangle A^{\prime} B^{\prime} C^{\prime}$ after rotating $\triangle A B C$ $180^{\circ}$ about the origin, then applying the dilation $(x, y) \rightarrow(3 x, 3 y)$ ?

33) Given $\triangle A B C$ and its image $\triangle D E F$. What series of transformations maps $\triangle A B C$ onto $\triangle D E F$ ?

A. Rotation $270^{\circ}$ clockwise about the origin followed by a reflection over the $y$-axis.
B. Reflection over the $x$-axis followed by a translation 5 units to the right and 2 units up.
C. Rotation $180^{\circ}$ clockwise about the origin followed by a reflection over the $x$-axis.
D. Reflection over the line $y=x$ followed by a rotation of $90^{\circ}$ clockwise about $C$.

## Transformations

34) Describe a congruence transformation that maps $\triangle A B C$ to $\triangle D E F$.

A. reflection in the $x$-axis, followed by a translation 4 units down.
B. reflection in the $x$-axis, followed by a translation 4 units up.
C. reflection in the $y$-axis, followed by a translation 4 units down.
D. reflection in the $y$-axis, followed by a translation 4 units up.
35) Describe a similarity transformation that maps $\triangle A B C$ to $\triangle D E F$.

A. reflection in the $x$-axis, followed by a dilation with a scale factor of 4 .
B. reflection in the $x$-axis, followed by a dilation with a scale factor of $\frac{1}{4}$.
C. reflection in the $y$-axis, followed by a dilation with a scale factor of 4 .
D. reflection in the $y$-axis, followed by a dilation with a scale factor of $\frac{1}{4}$.
36) The vertices of $\triangle P Q S$ are $P(7,6), Q(5,-3)$, and $S(-4,-8)$. What are the vertices of $\triangle P^{\prime} Q^{\prime} S^{\prime}$ after dilating from the origin by a scale factor of 3 , then translating up 2 units and left 9 units?

$$
P^{\prime}=\square \quad Q^{\prime}=\square \quad S^{\prime}=\square
$$

37) Given $\triangle A B C$ determine the coordinates of $\triangle A^{\prime} B^{\prime} C^{\prime}$ after a translation up 1 unit and left 2 units, followed by a dilation with center at the origin and scale factor 0.5 .

A. $A^{\prime}(-2,1), B^{\prime}(0,-2)$, and $C^{\prime}(1,2)$
B. $A^{\prime}(-2,2), B^{\prime}(0,-4)$, and $C^{\prime}(1,4)$
C. $A^{\prime}(-4,2), B^{\prime}(0,6)$, and $C^{\prime}(2,4)$
D. $A^{\prime}(-8,4), B^{\prime}(0,12)$, and $C^{\prime}(4,-8)$

## Transformations

38) Which transformations will map quadrilateral $P Q R S$ onto itself. Select All that apply.

A. Reflection over the $x$-axis.
B. Rotation $180^{\circ}$ clockwise about the origin.
C. Reflection over the line $y=0.5$.
D. Rotation $90^{\circ}$ clockwise about the origin.
E. Reflection over the $y$-axis.
F. Rotation $90^{\circ}$ counterclockwise about the origin.
39) Parallelogram PQRS is shown on the coordinate plane below. Which of these transformations will take parallelogram PQRS onto itself?

A. a reflection over the line $x=-5$
B. a reflection over the line $y=-5$
C. a rotation of $180^{\circ}$ clockwise about the center of the parallelogram.
D. a rotation of $360^{\circ}$ counterclockwise about the center of the parallelogram.
40) Which of these transformations map the figure onto itself? Select All that apply.
A. An equilateral triangle is reflected across a line coinciding with one of its sides.
B. A square is reflected across its diagonal.
C. A square is rotated $90^{\circ}$ clockwise about its center.
D. An isosceles trapezoid is rotated $180^{\circ}$ about its center.
E. A regular hexagon is rotated $45^{\circ}$ counterclockwise about its center.
41) Triangle $C A T$ has vertices $C(-9,9), A(-3,3)$, and $T(-6,0)$. If $\Delta B U G$ has vertices $B(-3,3), U(-1,1)$, and $G(-2,0)$. Is $\triangle C A T$ similar to $\triangle B U G$ ? If so, what transformation maps $\triangle C A T$ onto $\triangle B U G$ ?
A. No, dilation centered at the origin with scale factor of 3 .
B. No, dilation centered at the origin with scale factor of $\frac{1}{3}$.
C. Yes, dilation centered at the origin with scale factor of 3 .
D. Yes, dilation centered at the origin with scale factor of $\frac{1}{3}$.

## Transformations

42) The description of a sequence of transformations on a coordinate plane is shown.

A parallelogram is dilated by a scale factor of $\frac{1}{3}$ with the origin as the center of dilation. Then, it is reflected across the $x$-axis.

Which statements is true?
A. This sequence of transformations will preserve only the length of the sides.
B. This sequence of transformations preserves only angle measure.
C. This sequence of transformations preserves neither distance nor angle measure.
D. This sequence of transformations preserves both distance and angle measure.
43) Triangle $L K J$ is transformed on a coordinate plane to obtain triangle $L^{\prime} K^{\prime} J^{\prime}$. If the length of the corresponding sides is equal and the corresponding angles have the same measure, which of the following statements could be true? Select All that apply.
A. Triangle $L^{\prime} K^{\prime} J^{\prime}$ is the image of $\Delta L K J$ after a translation of 10 units up.
B. Triangle $L^{\prime} K^{\prime} J^{\prime}$ is the image of $\triangle L K J$ after a dilation with scale factor of -1 followed by a $180^{\circ}$ rotation.
C. Triangle $L^{\prime} K^{\prime} J^{\prime}$ is the image of $\Delta L K J$ after a dilation with scale factor 10 followed by a translation of 1 unit down.
D. Triangle $L^{\prime} K^{\prime} J^{\prime}$ is the image of $\Delta L K J$ after a reflection over the line $y=2 x$ followed by a rotation of $90^{\circ}$ about one of its vertices.
E. Triangle $L^{\prime} K^{\prime} J^{\prime}$ is the image of $\Delta L K J$ after a reflection over the line $y=-x$ followed by a dilation with scale factor of 0.3 .
44) In which case does the transformation of $\triangle Q R S$ result in an image $\triangle D E F$ where $\angle Q \cong \angle D, \angle R \cong \angle E, \angle S \cong \angle F$, and $\frac{Q R}{D E}=\frac{Q S}{D F}=\frac{R S}{E F} \neq 1$ ?
A. a translation of 6 units to the left and 8.5 units up followed by a reflection over the line $y=2 x$
B. a reflection over the line $y=-2 x$ followed by a translation of 6.5 units to the right and 3.5 units down
C. a rotation of $45^{\circ}$ clockwise about vertex $A$ followed by a dilation by a scale factor of 0.95 about the origin
D. a dilation by a scale factor of 1 about the origin followed by a rotation of $45^{\circ}$ clockwise about vertex $A$
45) Select all the transformations that preserve both distance and angle measure.
A. Reflection across the line $y=x$.
B. Translation of 3 units up.
C. Translation of 3 units up followed by a dilation with scale factor of 3 about point $(0,0)$.
D. Reflection across the line $y=x$ followed by a dilation with scale factor of -1 about point $(2,3)$.
E. Reflection across the line $y=-x$ followed by a dilation with scale factor of -0.5 about point $(1,1)$.

## Transformations

46) The figure below shows two perpendicular lines $n$ and $m$ intersecting at point $H$ in the interior of an isosceles triangle. Line $n$ bisects the base of the triangle. Which transformation will always carry the figure onto itself? Select All that apply.

A. a reflection across line $m$.
B. a reflection across line $n$.
C. a rotation of $90^{\circ}$ clockwise about point $H$.
D. a rotation of $180^{\circ}$ clockwise about point $H$.
E. a rotation of $270^{\circ}$ clockwise about point $H$.
F. a rotation of $360^{\circ}$ clockwise about point $H$.
47) Given $\triangle R S T$ and $\triangle X Y Z$. Which sequence of transformations shows $\triangle R S T \sim \Delta X Y Z$ ?

A. A dilation centered at the origin with scale factor of $\frac{1}{3}$ followed by a rotation of $270^{\circ}$ counterclockwise about point $T$.
B. A dilation centered at the origin with scale factor of 3 followed by a rotation of $270^{\circ}$ counterclockwise about point $T$.
C. A rotation of $270^{\circ}$ clockwise about the origin followed by a dilation centered at $R$ with scale factor of 3 .
D. A rotation of $270^{\circ}$ clockwise about the origin followed by a dilation centered at $R$ with scale factor of $\frac{1}{3}$.
48) Two figures are shown below.


Which of the following statements correctly explains whether or not the two figures are congruent?
A. The two figures are not congruent since the two figures are oriented differently.
B. The two figures are congruent since there is a rotation that carries one figure onto the other.
C. The two figures are congruent since there is a reflection that carries one figure onto the other.
D. The two figures are not congruent since there is no translation that carries one figure onto the other.

## Transformations

49) Which transformation preserves both distance and angle measure?
A. $(x, y) \rightarrow(2 x-4, y-6)$
B. $(x, y) \rightarrow(2 x-4,2 y-6)$
C. $(x, y) \rightarrow(-2 y+4, x-6)$
D. $(x, y) \rightarrow(-y+4, x-6)$
50) Square $A B C D$ is transformed to create the image $A^{\prime} B^{\prime} C^{\prime} D^{\prime}$, as shown in the figure below.


Select all the transformations that could have been performed.
A. a reflection across the line $y=x$
B. a reflection across the line $y=-x$
C. a rotation of 180 degrees clockwise about the origin
D. a reflection across the $x$-axis, and then a reflection across the $y$ axis
E. a rotation of 270 degrees counterclockwise about the origin, and then a reflection across the $x$-axis

